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### حساب المقطع العرضي للإلكترونات الضوئية لمدارات فرعية لذرة فوسفور في مركباته

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(قبل للنشر في 2002/9/18)

🗆 الملخّص 🗆

تعتمد شدة الإلكترونات الضوئية أو المساحة التي تشغلها هذه الخطوط على عدة عوامل منها: المقطع العرضي،عمق الانفلات للإلكترون ،نفوذية مقياس الطيف، عدم تجانس الطبقة السطحية للعينة.

لذلك، يهدف هذا العمل إلى حساب المقطع العرضي للإلكترونات الضوئية لمدارات فرعية في ذرة الفوسفور في بعض مركباته. بعد تحديد المقطع العرضي يمكننا تخمين احتمال إنتاج الكترون ضوئي في مدار فرعي لكل فوتون ساقط على العينة.

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# **1.Introduction:**

#### **Photoelectric cross – section :**

The term cross-section is used as a quantitative measure of an interaction between an incident particle and an atom.

The cross-sections per atom for a given process is defined through the probability, P= number of interactions /number of incident particles.

P=Nts (1)

Where N the number of atoms per unit volume in the target and t is its thickness.

The number of interaction for a target containing Nt atoms per unit area perpendicular to an incident beam of I particles is equal to INts .

Another unit of thickness is the mass absorption coefficient ( the product of the mass density  $D_m$  and the linear thickness t).

In this work we describe a calculation of the photoelectric cross-section using hydrogenic wave functions .

For this calculation we use an equation that is famous in quantum mechanics and is known as Fermi's Golden Rule[1].

Fermi's Golden Rule provides us the probability per unit time for a transition to the final state f from the initial state i between atom –orbits and is given by ,

$$W = \frac{2p}{h} D(E) \left| \left\langle y_{f} | H | y_{i} \right\rangle \right|^{2}$$
(2)

Where W is the transition rate and has dimension  $(time)^{-1}$ .

In this equation D(E) is the density of final states per unit energy.

Here, the three dimensional density of states is given by,

$$D(E) = \mathop{\underbrace{\overset{\text{e}}{\text{c}}}}_{\overset{\text{e}}{\text{c}}} \frac{V}{2p^2} \mathop{\overset{\text{e}}{\text{c}}}_{\overset{\text{e}}{\text{c}}} \frac{U}{h^2} \mathop{\overset{\text{e}}{\text{c}}}_{\overset{\text{e}}{\text{c}}} \frac{U}{h^2} \stackrel{\overset{\text{e}}{\text{c}}}{\overset{\text{e}}{\text{c}}} E^{\frac{1}{2}}$$
(3)

The most useful formula to calculate the probability of a transition comes from timedependent perturbation theory.

It's the formula which is the starting point for many of the derivations of cross-sections. Consider system with a Hamiltonian H given by,

$$H=H_{0}+H\phi$$
(4)

Where  $H_o$  is a time – independent operator and could be ,for example, the Hamiltonian which describes hydrogenic atom while H @may be a time – dependent perturbation.

$$\langle \mathbf{y}_{\mathrm{f}} | \mathbf{H} \langle \mathbf{y}_{\mathrm{f}} \rangle = \mathbf{\partial} \ast_{\mathrm{f}} \mathbf{H} \langle \mathbf{y}_{\mathrm{i}} dt = | \mathbf{H} \langle \mathbf{f} |$$
 (5)

Where y is the complex conjugate of y, dt is a three dimensional volume element.

X- ray photoelectron spectroscopy (XPS) is an example of a process that involves one atomic transition, the creation of an inner hole and an energetic photoelectron Fig.1.



Fig.1:Schematic diagram of X-ray photoelectron spectroscopy

The relevant wave functions for the initial and final states are given by,

$$y_{i}(r) = \frac{1}{\sqrt{pa}} e^{-r}$$

$$y_{f}(r) = \frac{1}{\sqrt{V}} e^{ikr}$$
(6)
(7)

where 
$$\mathbf{r} = \mathbf{r} / \mathbf{a}$$
,  $\mathbf{a} = \mathbf{a}_0 / \mathbf{Z}$ ,  $\mathbf{a}_0$  - Boher –radius ,Z- atomic number

The initial state  $y_i$  describes a ground state hydrogenic wave function in an atom and the final state  $y_f$  is usual outgoing plane wave normalized to a volume V.

In this calculation we assume the energy of the incoming photon **h**w on the target is more bigger than the binding energy  $E_B$  of the orbit-electron.

The transition probability can be calculated explicitly if the perturbation potential is

$$H'(z,t)=H'(z)e^{-i\mathbf{W}t}=-ez\mathcal{E}e^{-i\mathbf{W}t}$$
(8)

Where  $\mathcal{E}$  an applied electric field which acts on the particle in z direction.

From eqs.(2-8) we get W. The cross- section **s** is defined

as the ratio between W and the flux F of the incident electromagnetic radiation (the number of photons/area/time)[1].

$$s = W / F \tag{9}$$

The measurements for the binding energy of electrons were performed with XPS- method. By means of XPS-, a bound electron such as the K-shell electron promoted to a free state outside the sample, see Fig.1.

The kinetic energy of the photoelectron is well defined and sharp electron peaks appear in the spectrum.

In XPS, the sample is irradiated by constant photon energy hw and the kinetic energy of the electrons measured by means of spectrometer[2,3,4]. The relevant energy conservation equation is,

$$\mathbf{h}\mathbf{w} + \mathbf{E}_{\text{tot}}^{i} = \mathbf{E}_{\text{kin}} + \mathbf{E}_{\text{tot}}^{f} \left( \mathbf{K} \right)$$
(10)

Where  $E_{tot}^{i}$  is the total energy of the initial state,  $E_{kin}$  is the kinetic energy of the photoelectrons, and  $E_{tot}^{f}$  is the total energy of the system after ejection of the photoelectron from the K- level.

The binding energy of the photoelectron is defined as the energy required to remove it to infinity with a zero kinetic energy.

$$\mathbf{h}\mathbf{w} = \mathbf{E}_{\rm kin} + \mathbf{E}_{\rm B}^{\rm V}(\mathbf{k}) \tag{11}$$

Where  $E_B^V(K) = (E_{tot}^f - E_{tot}^i)$  is the binding energy of an electron in the K-level referenced to the local vacuum level. In the solid state, the Fermi-level is used as a reference niveau. Then,

$$\mathbf{h}\mathbf{w} = \mathbf{E}_{\mathrm{kin}} + \mathbf{E}_{\mathrm{B}}^{\mathrm{F}}\left(\mathbf{K}\right) \tag{12}$$

In this work we consider the case that  $hw >> E_B$ , so that E @hw. Under this condition the final results for the photoelectric cross-section  $s_{ph}$  yields,

$$\mathbf{s}_{\rm ph} = \frac{7.75}{\mathbf{hw}} \stackrel{\mathbf{c} \in \mathbf{E}_{\rm B}}{\mathbf{c}} \stackrel{\mathbf{c}^{2}}{\mathbf{hw}} \stackrel{\mathbf{c}^{2}}{\mathbf{c}} \qquad \mathbf{A}^{2}$$
(13)

From (13) we notice that  $s_{ph}$  decreases with increasing photon energy  $as(hw)^{5/2}$ .

Electron Impact Ionization Cross-Section :

The cross-section for an inelastic electron-electron collision  ${}^{S}$   ${}^{e}$  can be derived by using impulse approximation for scattering in central force field. Then,  ${}^{S}$   ${}^{e}$  is given by,

 $s_e = p e^4 / EE_B$ ;  $E \tilde{n} E_B$  (14)

Where E the energy of the incident electron beam and  $E_B$  is the binding energy of orbital –electron .

### 2. Results

during the XPS measurements the specimens were irradiated with Al  $K_a(hu) = 1486.6eV$  to obtain  $P_{2s}$ ,  $P_{2p}$ -binding energies.

Nr	Sample	$E_B(P_{2s})$	$E_B(P_{2p})$
1	Р	188.25	130.65
2	InP	188.5	128.85
3	GaP	187.05	129.4
4	Na <sub>3</sub> PO <sub>4</sub>	190.15	132.75
5	NH <sub>4</sub> PF <sub>6</sub>	194.8	137.65

Table 1 contains 5 samples of phosphorus and  $P_{2s}$ ,  $P_{2p}$  - binding energies in eV[5].

Table 1: contains samples,  $P_{2s}$  ,  $P_{2p}$  –binding energies. All values are given in eV

The calculation of  ${}^{s}$   ${}^{ph}$  of phosphorus-subshells are presented in table 2 according to eq. (13).

In addition, table 2 illustrates ,for comparison, values of  ${}^{S}{}_{e}$  according to eg.(14) with supposing the electron beam energy is the same as the energy of the  $K_{a}$  - photons.

Nr	$s_{ph}(P_{2s})$	$s_{ph}(P_{2p})$	$\mathbf{s}_{e}(\mathbf{P}_{2p})$	C [6]	Dc
1	2.85	1.14	335.19	2.19	0
2	2.79	1.10	340.10	1.78	-0.41
3	2.81	1.12	338.86	1.81	-0.38
4	2.93	1.19	330.10	3.44	1.25
5	3.11	1.30	318.34	3.95	1.76

Table 2 : contains cross-section S  $(10^{-21} \text{ cm}^2)$ , electronegativity C and electronegativity difference DC between P and its adjacent –atoms.

Numbers correspond to compounds listed in table 1

## **3.** Discussion

From table 2 we notice that the shifts of the cross-section between P-compound are small . Thereby , one infers that the environment of phosphorus couldn't have affects on the s $_{\rm ph}$ Fig.2 .

As expected, the dependence has weak effects on the cross-section[7].



Fig.2. The dependence of S <sub>ph</sub> on the difference in Pauling's electronegativity DC between phosphorus and the neighbourig atoms.

From Fig.3 one can see a linear relationship between  $s_{ph}(P_{2p})$  and  $s_{ph}(P_{2s})$ .

This relation reflects a stronger interaction of the 2s-subshell with the incident radiation in contrast to the 2p-subshell.



As can be seen from Fig.4 the  $s_{e}$  values are always larger than the corresponding  $s_{ph}$  values, as electrons are charged particles in comparison with photons.



$$s_{e}(P_{2p})' 10^{-21} \text{ cm}^{2}$$

$$s_{ph}(P_{2p})$$
,  $10^{-21} cm^2$ 

Fig.4: Comparison of S  $_{\rm ph}\,$  with S  $_{\rm e}$ 

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